

Looking At Some Data from Isard's "Methods of Regional Analysis"

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In his path-breaking book “Methods of Regional Analysis” (MIT Press, 1960) Walter Isard presented several sets of data. Some of these are fictitious, designed to illustrate concepts. Others contain real empirical values. Among the latter are several tables. I have used two of these, not in a research mode, but rather as exploratory visualizations. Of the two matrices one is 36 by 36 in size, the other is 47 by 47. I have used these tables in their original form without attempting any transformations such as biproportional adjustment to equalize marginals, or eigenvector analysis, or partitioning into symmetric and skew symmetric parts to estimate potentials¹. Nor have I attempted to reduce the resolution of the data by combining, or by omitting, rows or columns from the matrices.

Relating to the first of my examples, Isard has four maps of the movement of funds between Federal Reserve cities. These are illustrated on pages 149, 154-156. of the book. He also presented a table² of similar monetary transfers between the thirty-six Federal Reserve cities in the United States. Curiously none of the four maps shown is made using the information from this table. But he argued, rightly in my opinion, that such tables and maps should be used more widely. To date I have not seen much evidence that this suggestion has been followed. An examination of recent issues of the *Annals of Regional Science* convinces one of this fact. Isard thus recognized that insufficient use is often made of the human power of inference from visualizations in research. As an exercise to demonstrate the usefulness of this idea I have used a simple and freely available computer program³ to create several maps from the 36 by 36 table. In order to do this it was only necessary to look up the latitudes and longitudes of the cities on the internet and to find a computer compatible outline map of the United States. The preparation of such maps is then very simple and alternate versions of the maps can be created quickly. The computer program allows one to interactively hover (with a mouse) over a location to read its name, and to hover over the flow symbol to be presented with the numerical value. Thus exploratory research use can be made of the maps. This interaction of course is not possible with the printed versions of the maps⁵.

The thirty six by thirty six matrix yields a possible 1,260 movements so that some parsing is desirable. Such tables are not random, but contain considerable structure. The majority of the volume is contained in a minority of the flows so that deleting flows below the mean tends to leave 75% of the movement volume but requires only 20% of the movement activity. This is a far better strategy than, for example, reducing the resolution by lumping all of the

thirty six cities into the twelve Federal Reserve Districts and thereby reducing the 1260 values to 132 with the attendant loss of geographic detail.

Examples of maps from one set of data hardly constitutes a research project – but inclusion of such fiscal-movement maps can enhance most studies, and a sequence from several time periods is certain to be enlightening, especially if rendered within an animation.

Click on the links below, inside the red rectangles, to see the images.

Map 1: Original map from Isard, p.149.

Table I (part), from Isard.

Map 2: All fiscal transfers during a week (of 1,260 possible)

Map 3: Net transfers greater than 2×10^7 dollars

Map 4: Above average transfers to New York City

Map 5: Above average transfers from New York City

Animation of Maps 1 to 5, above [Ed.].

Another important data array is available in an input-output table. As pointed out by Isard⁴ “...the *interregional input-output* approach is most prominent, both in terms of accomplishment and recognition. It represents a fruitful approach for depicting and investigating the underlying processes which bond together the regions of a system and all the separate facets of their economies.” A graphical exercise, similar to that given above, has been undertaken with respect to the New England input/output table from the “Methods” book⁶. In this case there are forty-seven industry groupings and the flows are represented by a 47 by 47 table. The industries are quickly given coordinate locations by a metric multidimensional scaling program⁷. This works somewhat as follows. Consider two industries to be “close” if the quantity of exchanges between them is large. Then construct a diagram in which “close” industries are placed near each other. Do this by positioning a first industry at random. Take the industry “closest” to this and place it on a circle of chosen radius near the first one, thereby establishing a scale for the diagram. The next industry, the third industry, then lies at the intersection of two circles drawn about the first two, with appropriately scaled radii. There is a slight ambiguity and arbitrariness here because two circles can intersect in two places. Choose one of the options and insert the third industry. and then proceed to locate the next (fourth) industry using more circles. The degrees of freedom rapidly decrease and the choices become more difficult. Mathematically the fitting via

circles can be replaced by an iterative procedure that places industries into the diagram so that “close” industries are also close in the diagram⁸. The contacts between industries are then drawn as flows between these locations using the same mapping computer program. Curiously the scaling algorithm has placed most of the industries on the perimeter of a circle with only a few industries in the interior. My suspicion is that the starting configuration - the Gower algorithm was used - began with all items on a circle. The non-metric version - the Torsca algorithm - gave very similar results.

The few interior-lying industries seem to dominate the table. The “Household” category is especially prominent. The important industries exchanging goods and services are easily identified when using the interactive computer program, as are the magnitudes involved. Close visual examination of the original input-output matrix would permit recognition of these major flows, especially when studied by the original compiler of the table. But without such close scrutiny a casual user could find the graphical version(s) more useful and especially rapid. This technique has, to the best of my knowledge, not been used very often, if at all, with input/output tables.

The 47 by 47 matrix could contain as many as 2,162 entries, if the diagonal is ignored, so that a parsing by size is again appropriate, as is seen clearly in the diagrams. Only a little over a dozen entries are significant. As is the case with the movement maps, one example does not constitute a research project but a series of such diagrams, even an animation, can enhance the study of changing regional structure. An opportunity to study regional dynamics thus becomes available. An interesting experiment might be provided by applying the technique to the Leontiev inverse, or to the input/output coefficient matrix.

Click on the links below, inside the red rectangles, to see the images.

Table 3 (part), from Isard.

Map 6: The complete I/O table in graphic form

Map 7: All exchanges above the average

Map 8: Above $5 * 10^8$ dollars, with labels

Map 9: Net exchanges above $2 * 10^7$ dollars

Citations

¹ W. Tobler, 2005, "Estimation of Potentials from Asymmetries", in Solstice, A refereed electronic journal, XVI, 2 (Winter) at: <http://www.imagenet.org>

² "Table 1. Net Commercial And Financial Flows Between Federal Reserve Zones, Week Ended October 13, 1954", pages 152-153 of W. Isard, 1960, Methods of Regional Analysis, Cambridge, MIT Press. Careful examination of Isard's table and the maps reveals that they came from different sources and relate to different time periods. Thus the flows mapped here differ from those illustrated in the book.

³ The program, tutorial, and sample data can be downloaded without charge from: [www.csiss.org/spatialtools/flow mapper](http://www.csiss.org/spatialtools/flowmapper)

⁴ An alternate graphical method of representing dollar movement is presented in W. Tobler, 1981, "A Model of Geographic Movement", Geographical Analysis, 13, 1 (Jan):1-20; Table I, Figures 1-6..

⁵ Isard, op. cit., 310; emphasis as in the original.

⁶ "Table 3. New England: Input Requirements And Commodity Balances, 1947, Estimated from National Coefficients", pages 604-607 of Isard, 1960, op. cit. Also see the discussion of the data in the table on pages 603-617.

⁷ Borgatti, 1996, ANTHROPAC 4.0, Natick, MA, Analytic Technologies. The two-dimensional stress after eight iterations was 0.40. A three dimensional solution was not attempted.

⁸ A simple introduction to one of the iterative methods is given in: W. Tobler, 1996, "A Graphical Introduction to Survey Adjustment", Cartographica, 33-42.